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防帳卡號被盜之低成本免憑證電子錢網路付款可行性方案 研究

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- 中 文 摘 要 : 安全的電子付款工具在 B2C 或 C2C 電子商務中扮演很重要的角色。
- 中文關鍵詞: 電子錢,匿名性,匿名撤銷,身分盜用,金融卡盜刷
- 英文摘要: Secure electronic payment instruments play an important role in retail electronic commerce. As in most countries, people in Taiwan often use credit cards for payments on Internet shopping. However, the information contained in the card includes sensitive data like card number, valid date, and CVC (Card Verification Code) which all easily suffer data leakage, or impersonation attacks. This may cause the banks, merchants, or user to suffer serious losses. In this paper, we propose an ID-based untraceable electronic cash without card number or personal information to mitigate the risk of data leakage. Meanwhile, our method also considers preventing the anonymity abuse and adds the function of anonymity revocation through a trust party. In addition, due to the proposed is an ID-based scheme, it has the advantage of PKI (Public Kev Infrastructure) free and thus save the certificate management cost.
- 英文關鍵詞: Electronic Cash, Anonymity, Anonymity Revocation, Identity Theft, Financial Card Fraud

# FINAL REPORT

ID-Based Certificateless Electronic Cash on Smart Card against Identity Theft and Financial Card Fraud

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# Abstract

Secure electronic payment instruments play an important role in retail electronic commerce. As in most countries, people in Taiwan often use credit cards for payments on Internet shopping. However, the information contained in the card includes sensitive data like card number, valid date, and CVC (Card Verification Code) which all easily suffer data leakage, or impersonation attacks. This may cause the banks, merchants, or user to suffer serious losses. In this paper, we propose an ID-based untraceable electronic cash without card number or personal information to mitigate the risk of data leakage. Meanwhile, our method also considers preventing the anonymity abuse and adds the function of anonymity revocation through a trust party. In addition, due to the proposed is an ID-based scheme, it has the advantage of PKI (Public Key Infrastructure) free and thus save the certificate management cost.

**Keywords**: electronic cash, anonymity, anonymity revocation, identity theft, financial card fraud

# Content

1	INTRODUCTION	4
2	BACKGROUND KNOWLEDGE OF ELECTRONIC CASH	6
3	SECURITY RATIONALES	8
3.1	Intractable Problems and Assumptions	8
3.2	Bilinear Pairing	9
3.3	BLS Signature	9
3.4	Secure Hash Function	10
4	THE PROPOSED SCHEME	11
5	SYSTEM ANALYSIS AND EVALUATION	15
6	IMPLEMENTATION	20
7	CONCLUSION	22
RE	FERENCE	23
AP	PENDIX	26
I	Main Program	26
п	Program Running Result	35

### 1 Introduction

Internet shopping nowadays has become an important consumption channel for people's daily life. However, it might make the consumer unsatisfactory about personal data leakage, identity theft and transactions' unsafety. According to an investigation in Taiwanese e-commerce yearly book 2011, the most frequent used payment tools for online shopping are: online credit card payment (74.6%), WebATM (i.e. online Automatic Teller Machine) account transfer (52.8%), physical ATM account transfer (46.6%), payment after shipment (37.5%), convenient store payment (37.5%), respectively. So, there are about three quarters of Taiwanese consumers experiencing online credit card payments. This is because Taiwanese have been familiar with the credit cards payments in physical stores, and the credit card usage is usually encouraged by bonus activities sponsored by the companies. In addition, online credit card payment does not require a card reader while compared with the WebATM account transfers in Taiwan. It only needs the consumers to input card number, CVC (Card Verification Code) and the valid date of the card. However, all these personal information can easily suffer data theft. For example, the customer's personal computer is likely to be embedded with Trojon horses to steal the data, and the keystrokes, communication packets and computer screens are also likely to be skimmed. Moreover, if the merchant websites are not properly managed, the transaction data will easily become the targets for criminals. According to a report from Taiwan Joint Credit Information Center, the percentage of online credit card frauds in the total credit card frauds is 40% in 2009, but it rises to 60% rapidly in the third quarter of 2011. Compared to the serious threat of online credit card frauds, WebATM payment has a lower risk in this aspect. This is because WebATM payment requires the consumer to insert his/her debit card into a card reader, which is connected to his/her own personal computer or notebook, and then enter his/her password through the keypad to enable account transfer. Such a solution builds a defense against Trojon horses stealing users' password [1]. However, users' bank accounts are still clearly transferred on the open network.

The above two most frequently used online payment tools in Taiwan are account-based. Both require the payer to provide personal identifiable information for the financial institutes to confirm the payments. From this, it can be easily seen that the card number / account number and the necessary individual information all need to be transferred on the net. This naturally brings the risk of data leakage or theft. To cope with the problem, untraceable electronic cash (e-cash) which contains no information about individuals was developed to resist both personal data theft and

identity theft [2]. It typically composes of a series of random bits and a bank's signature, and therefore cannot be linked to any personal accounts.

However, the digital signature in the e-cash needs to use a public key cryptosystem, such as RSA, the most frequently used scheme. In that, the public key composes of a series of meaningless binary digits. For example,

Public exponent:

0x10001

Modulus:

13506641086599522334960321627880596993888147560566702752448514 38515265106048595338339402871505719094417982072821644715513736 80419703964191743046496589274256239341020864383202110372958725 76235850964311056407350150818751067659462920556368552947521350 08528794163773285339061097505443349998111500569772368909275623

In commercial applications, a meaningless RSA public key requires using a meaningful certification to link to a user's identity. It requires additional overhead to handle the certification management. For this reason, an ID-based cryptosystem was proposed which no longer demands the certification because of its using user identification as the public key. For example

Public key:

Alice@xxx.com

The advantages of an ID-based public cryptosystem are that it requires neither PKI nor certification management, such as certificate enquiry, revocation, renewal, and so on. The purpose of this paper is to implement such an ID-based untraceable electronic cash to prevent personal data leakage and achieve more efficient public key usage. The organization of the remaining paper is as follows. The background knowledge is introduced in Section 2. Some security rationales are described in Section 3. Section 4 shows our proposal. Section 5 discusses its security and performance. Finally, a conclusion is given in Section 6.

#### 2 Background Knowledge of Electronic Cash

Electronic cash (e-cash) like paper money can allow payers to pay without being traced. There have been many cryptographic scientists working within the field of e-cash system design [3-20] since Chaum first proposed the concept in 1982 [3].

From the control viewpoint, e-cash systems fall into two categories: (1) bank-controlled and (2) P2P (peer-to-peer) -distributed. A bank-controlled e-cash system typically contains three roles: customer, bank and merchant, and three protocols: withdrawal, payment, and deposit. As a required function of an untraceable e-cash system, when a customer withdraws e-cash from an issuing bank and pays it to a merchant, and then the merchant deposits it at an acquiring bank, no one can link the e-cash to the customer. This is referred to as anonymity or untraceability. The main underlying technique is the blind signature scheme. Mondex [21] is one of the bank-controlled systems, produced by National Westminster Bank in the U. K., and has a great success in 1990s. It has absolute anonymity, but at the same time opens a perfect channel for criminals to untraceably transfer their illegal funds. On the other hand, P2P distributed e-cash system kills the role of central bank or authority and thus reduces the expensive bank-processing cost. Bitcoin [22-24] is a famous P2P distributed e-cash system and has been reigning over the cyberspace in the real world. All activities, including coin mintage, coin validness check, double-spending check, are done through the cooperation of the peer nodes on the Bitcoin P2P network. By just generating a public/private key pair, a user can join the Bitcoin network, and use the public key as his/her pseudonym to mine, exchange, buy, and spend the Bitcoin without revealing his/her real identity and location. Nevertheless, some privacy issues emerge because of the public transactions. For instance, one may trace sensitive transactions or de-anonymous social network data through using network topology, and thus violating users' privacy [25, 26].

To be a sound cash system, some essential properties should be centralized.

- Verifiability: The e-cash validity can be publicly examined.
- **Unforgeability:** E-cash should be issued only through specialized procedures. No one, including banks, can forge e-cash by any other ways.
- Untraceability (or unlinkability): It means that no one, including the bank, can know the e-cash owner when the cash is used legally. Although, the bank provides e-cash withdrawal service to its account holder, it cannot link any e-cash to the holder's identity.
- **Double-spending detection**: An e-cash system should prevent e-cash from double spending. If this occurs, the system should be able to get the cheater

efficiently.

• Anonymity revocation: When e-cash is illegal used such as, money laundering and tax evading, the system should has the ability to reveal its owner. An e-cash system with anonymity revocation is called fair e-cash system.

For fair e-cash systems [6, 10, 11, 15, 16, 19, 20], an additional trustee is involved in the escrow of some critical information, such as linking the owner's identity to the e-cash. Once a bank or a law enforcement agency requests anonymity revocation, the trustee can reveal the e-cash owner. In other words, the anonymity of e-cash is maintained if the e-cash is used legally, but is revoked if misused.

Pairing-based cryptography is greatly applied in various applications for latest two decades, because it is easier to design an ID-based cryptosystem and requires only about one sixth key length compared to RSA-based cryptosystems. There have been several pairing-based fair e-cash systems proposed. The work of Hufschmitt and Traoré [27] is provably secure, but needs many underlying building blocks (including bilinear pairing, Paillar encryption, double ElGamal encryption, and Fiat-Shamir heuristic) which make it very complicated. Fuchsbauer et al.'s fair e-cash [12], like Hufschmitt and Traoré's, is also a complex construction, because it uses public encryption primitive to achieve e-coin's blindness, and employs both commitment technique and zero-knowledge proof to ensure the encrypted content is well-constructed so as to let the inside tracing information can be disclosed when anonymity revocation is demanded. In addition, the underlying signature scheme (constructed from group signature) is also in complex concept. On the other hand, three pairing-based e-cash systems, Popescu and Oros' [28], Wang et al.'s [29], and Chen et al.'s [30], make their e-cash include a trustee-issued certificate which can be linked to e-cash owner only by the trustee himself. However, Chen et al. pointed that Popescu and Oros' scheme violates anonymity, and Wang et al.'s has a deficiency in that a malicious user can use an unregistered certificate to withdraw e-cash from a bank. Until now Chen et al.'s scheme [30] is the most efficient pairing-based fair e-cash systems among the above-mentioned, but it has two weaknesses. First, its security is not formally proved. Second, the blind factor used for protecting the message to be signed is always the same if the user employs the same certificate to withdraw e-cash.

# **3** Security Rationales

This section defines several terminologies used in this paper.

#### 3.1 Intractable Problems and Assumptions

A major goal of cryptographic applications is to create a secure cryptographic scheme such that breaking the scheme can be reduced to solving an **intractable problem**. Formally, problems that can be solved in theory (e.g., given infinite time), but taking too long for their solutions to be useful in practice, are known as **intractable problems**. In complexity theory, a problem is **intractable** if no **probabilistic polynomial-time** (**PPT**) adversary can solve it with **non-negligible** probability. Followings are some intractable problems and assumptions related to elliptic curve cryptography [31, 32] used in this study. In them, we let *G* be an additive elliptic-curve group with prime order *q* and a base point *P*.

**Definition 2.1 The Discrete Log (DL) Assumption** states that the following problem is  $(\tau, \varepsilon)$ -intractable: given a group  $G = \langle P \rangle$  and a random point  $Q \in G$ , find the integer *a* 

 $\in Z_a^*$  such that Q = aP, by taking at most time  $\tau$  with a **negligible** probability  $\varepsilon$ .

**Definition 2.2 The Computational Diffie-Hellman (CDH) Assumption** states that the following problem is  $(\tau, \varepsilon)$ -intractable: given a group  $G = \langle P \rangle$  and two random points *aP* and *bP*  $\in$  *G*, compute *abP*, with at most time  $\tau$  and probability  $\varepsilon$ , if  $\varepsilon$  is **negligible**.

**Definition 2.2 The Variant Computational Diffie-Hellman (VCDH) Assumption** states that the following problem is  $(\tau, \varepsilon)$ -intractable: given a group  $G = \langle P \rangle$ , and three random points Q, aQ and  $bQ \in G$ , compute abQ, with at most time  $\tau$  and probability  $\varepsilon$ , if  $\varepsilon$  is **negligible** [33].

Koblitz and Menezes [32] pointed out that the **DL** and **CDH** problems on a sufficiently large group are regarded as classical intractable problems. Rather, the **Decisional Diffie-Hellman (DDH)** problem — given three random points aP, bP, and  $cP \in G$ , decide whether  $c = ab \pmod{q}$  — is believed to be **intractable** on any suitable group, except for the **gap Diffie-Hellman (GDH)** group in which there exists an efficient **bilinear pairing** function. That is, the **DDH** problem on a **GDH** group can be solved in polynomial time through **bilinear pairing**; we will describe this in

the following section.

#### 3.2 Bilinear Pairing

Weil pairing [34, 35] is a tuple  $(G_1, G_2, q, P, \hat{e})$  where  $(G_1, +)$  and  $(G_2, \cdot)$  are two cyclic groups of order q, P is a generator of  $G_1$ , and  $\hat{e}: G_1 \times G_1 \rightarrow G_2$  is a mapping which has the following properties:

- 1. Bilinearity: If *a*, *b* are two integers and *P*,  $Q \in G_1$ , one has  $\hat{e}(aP, bQ) = \hat{e}(P, Q)^{ab}$ .
- 2. Non-degeneracy: If P is a generator of  $G_1$ , then  $\hat{e}(P, P)$  is a generator of  $G_2$ .
- 3. Computable: There is an efficient algorithm to compute  $\hat{e}(P, Q)$  for any  $P, Q \in G_1$ .

An important result is that **Weil pairing** allows us to determine whether points aP, bP, cP in  $G_1$  satisfies  $ab = c \mod q$ , i.e.

$$ab = c \mod q$$
 iff  $\hat{e}(aP, bP) = \hat{e}(P, cP)$ .

In other words, for solving a **DDH** problem one requires only two evaluations of the **Weil pairing** for points in  $G_1$ . That is why the group  $G_1$  is referred to as a **GDH** group because of the difference in difficulty between **CDH** and **DDH** problems in the group.

#### 3.3 BLS Signature

Boneh, Lynn, and Shacham [35] proposed a short signature scheme, **BLS** in brief, from **Weil pairing** in 2001. The signature length is half the size of a DSA signature for a same security level, and the scheme should be constructed over a **GDH** group. **BLS** comprises the following system settings and some algorithms: **KeyGen**, **Sign**, and **Verify**.

- System settings: The system parameters (G<sub>1</sub>, G<sub>2</sub>, P, q, ê) are the same as the ones in Section 2.2, In addition, the system makes use of a hash algorithm H: {0, 1}\* → G<sub>1</sub>, mapping a string to a point in G<sub>1</sub>.
- KeyGen algorithm: This algorithm picks a random number  $x \in Z_q^*$  as the signing key and computes the corresponding verification key X = xP, which is a point in  $G_1$ .
- Sign algorithm: To sign on a message  $m \in \{0, 1\}^*$ , compute signature S = xH(m), and output *S*.
- Verify algorithm: On inputting message m and its signature S, one can use the

verification key X to verify S by examining whether (P, X, H(m), S) is a Diffie-Hellman tuple. In other words, one can check whether the equation  $\hat{e}(X, H(m)) = \hat{e}(P, S)$  holds.

The **BLS** signature scheme is provably secure under the intractability of the **CDH** assumption.

#### 3.4 Secure Hash Function

A hash function H(.) is a transformation that takes a variable-size input m and returns a fixed-size string, which is called the hash value h (i.e., h = H(m)) or the *digest* of message m. A secure hash function [36] must be able to withstand all known types of cryptanalytic attacks. At a minimum, it must have the following properties:

- 1. Pre-image resistance: Given h, it should be computationally infeasible to find any message m such that h = H(m). This concept is called a **one-way** property.
- 2. Second-pre-image resistance: Given an input  $m_1$ , it should be computationally infeasible to find another input  $m_2$ , where  $m_1 \neq m_2$ , such that  $H(m_1) = H(m_2)$ . This property is referred to as weak collision resistance.
- **3.** Collision resistance: It should be computationally infeasible to find two different messages  $m_1$  and  $m_2$ , such that  $H(m_1) = H(m_2)$ . Such a pair is called a cryptographic hash collision. This property is called strong collision resistance.

### 4 The Proposed Scheme

Our design goals are to propose a fair untraceability e-cash system and to minimize user side computations. The proposed system has four parties: trustee T, bank B, user U, and merchant M, and five protocols: license issuing, withdrawal, payment, deposit, and owner tracing. We assume that T is a trust third party. (To prevent the collusion, the private key of T can be separated into several shares held by different authorities through a share-secrecy technique.) The following details the system initialization and the five protocols. The notations are listed in Table 1 and the protocols are illustrated in Figure 1.

**Initialization.** The trustee *T* publishes system parameters { $G_1$ ,  $G_2$ , P, q,  $\hat{e}$ , H}, as defined in Section 3.2. It also publishes a mapping function  $H_1$  which maps {0, 1}<sup>\*</sup> to  $G_1$ . In addition, bank *B* registers its private key  $x \in Z_q^*$  and its identity with a valid date,  $ID_{BV} = ID_B ||VD_B$ , to the trustee *T*. *B* then obtains  $Q_B = H_1(ID_{BV})$ ,  $P_B = xQ_B$  and  $SIG_T(Q_B ||P_B)$ , where  $SIG_T(Q_B ||P_B)$  is the trustee's signature on  $Q_B ||P_B$ . Then, bank *B* makes the information,  $ID_{BV}$ ,  $P_B$  and  $SIG_T(Q_B ||P_B)$ , public.

x	Bank's private key		
$ID_{BV}$	bank's pubic data indicates the bank's identity		
	together with a valid period.		
$Q_B$	$Q_B = H_1(ID_{BV})$ is bank's public data		
$P_B$	$P_B = xQ_B$ is bank's public data		
SIG <sub>T</sub> (.)	Trustee $T$ 's signature on some message		
W	A user-chosen license key		
$Q_L$	$Q_L = wP_B$ is a license for e-cash		
SK	a session key shared between a user and a		
	merchant in a payment transaction		

Table 1 Notations in the proposed scheme

**License issuing protocol.** Once a user U who is an account holder of a bank B wants to employ e-cash as a payment tool, he/she should apply for a license to the trustee T in advance. U and T together do the following steps.

- (1) *U* randomly chooses a **license key**  $w \in Z_q^*$  and sends it with his/her bank's name to *T* through a secure and authenticated channel (e.g., they have performed mutually authentication and session key exchange in advance.).
- (2) *T* fetches the bank's public information  $ID_{BV}$ ,  $Q_B$  and  $P_B$  from its database.

- (3) *T* computes a **license** as  $Q_L = wP_B$  and then signs the license as SIG<sub>T</sub>( $Q_L$ ). *T* stores {*U*,  $Q_L$ } into its database and returns { $Q_L$ , SIG<sub>T</sub>( $Q_L$ ),  $ID_{BV}$ ,  $P_B$ } to *U*.
- (4) On receiving the message, U confirmes the validness of  $Q_L$  by examining the T's signature SIG<sub>T</sub>( $Q_L$ ). If it is valid, U stores {w,  $Q_L$ , SIG<sub>T</sub>( $Q_L$ ),  $ID_{BV}$ ,  $P_B$ } into his/her smart card.

Withdrawal protocol. After having a valid license, a user U can withdrawal e-cash from his/her bank B. The detail steps between U and B are described below.

- (1) *U* selects a random e-coin *c*, a random element *R'* in *G*<sub>1</sub> and two blind factors  $a, b \in Z_q^*$  such that  $ab = w \mod q$ , where *w* is *U*'s **license key**. *U* then computes a blind message  $M = b(H(c||R||ID_{BV}) + R)$  and sends *M* to *B*.
- (2) *B* performs blind signing, S' = xM, by using its private key *x*, and then returns the blind signature *S'* to *U*.
- (3) *U* unblinds the received S' by computing S = aS' and R = wR', and obtains e-cash  $\{c, S, R\}$ .

Here, the proposed e-cash verification equation is

$$\hat{e}(H_1(ID_{BV}), S) =? \hat{e}(Q_L, H(c||R||ID_{BV})) \hat{e}(P_B, R).$$
 ..... Eq.(1)

We show the proof below.

 $\hat{e} (H_1(ID_{BV}), S) = \hat{e} (Q_B, S) = \hat{e} (Q_B, aS') = \hat{e} (Q_B, axM) = \hat{e} (Q_B, axM) = \hat{e} (Q_B, axb(H(c||R||ID_{BV}) + R')) = \hat{e} (Q_B, wxH(c||R||ID_{BV})) \hat{e} (Q_B, wxR') = \hat{e} (wxQ_B, H(c||R||ID_{BV})) \hat{e} (xQ_B, R). = \hat{e} (wP_B, H(c||R||ID_{BV})) \hat{e} (P_B, R). = \hat{e} (Q_L, H(c||R||ID_{BV})) \hat{e} (P_B, R).$ 

**Payment protocol.** After purchasing, a user U wants to pay a merchant M with the e-cash in his/her smart card. Suppose that the e-cash left is d and the amount to be paid is m, where  $d \ge m$ . U and M will do the followings:

- (1) U sends e-cash and the corresponding data,  $pmsg = \{c, S, R Q_L, SIG_T(Q_L), ID_{BV}, P_B\}$  to M.
- (2) On receiving the message, *M* confirmes the validness of *Q<sub>L</sub>* by examining *T*'s signature SIG<sub>T</sub>(*Q<sub>L</sub>*). If it is valid, *M* makes a challenge, *K*, by randomly selecting an integer k ∈ Z<sup>\*</sup><sub>q</sub> and computing K = kP<sub>B</sub>, and sends K to U.

- (3) On receiving the challenge K, user U computes SK = wK = wkP<sub>B</sub> and the owner-signature S<sub>m</sub> = wH(SK||t||m) using license key w, where t is the current time. U then decreases e-cash balance in the smart card by \$m, stores {t, m, K} into the smart card, and sends {t, m, S<sub>m</sub>} to M.
- (4) On receiving { $t, m, S_m$ }, M computes  $Q_B = H_1(ID_{BV})$  and  $SK' = kQ_L = kwP_B$ . M then verifies whether the payer U is the owner of license  $Q_L$  by checking  $\hat{e}(P_B, S_m) = ?\hat{e}(H(SK||t||m), Q_L)$ . If the equation holds, M verifies whether the e-cash is valid by checking  $\hat{e}(Q_B, S) = ?\hat{e}(Q_L, H(c||R||ID_{BV}))\hat{e}(P_B, R)$ . If both checks passed, M stores a **payment record**, { $c, S, R Q_L, SIG_T(Q_L), ID_{BV}, P_B, k, t, m, S_m$ }, into its database.

License issuing: User	Trustee T
1.Selects license key $w \in Z_q^*$ .	w, BankName
	2. Fetchs the bank's pubic data $ID_{BV}, Q_B, P_B$ .
	$Q_L$ , SIG <sub>T</sub> ( $Q_L$ ), $ID_{BV}$ , $P_B$ 3. Computes $Q_L = wP_B$ , SIG <sub>T</sub> ( $Q_L$ ).
4. Verifies $Q_L$ with SIG <sub><i>T</i></sub> ( $Q_L$ ) and	
Stores { $w, Q_L, SIG_T(Q_L), ID_{BV}, P_B$ }	
Withdrawal:User1. Selects $c, R' \in G_1, a, b \in Z_q^*$	Bank B
such that $ab = w \mod q$ , and	
computes $M = b(H(c  R  ID_{BV})+R)$ .	
	S' 2.Computes $S' = xM$ .
3. Computes $S = aS'$ , $R = wR'$ , and	
obtains $e$ -cash={ $c, S, R$ }.	
Payment: User	Merchant M
(Note: $t$ - current time, $m$ – paid money)	
$1.pmsg = \{c, S, R, Q_L, \text{SIG}_T(Q_L), ID_{BV}, P_B\}$	pmsg
	2. Verifies $Q_L$ with SIG <sub><i>T</i></sub> ( $Q_L$ ).
	Selects $k \in \mathbb{Z}_q^*$ , and computes
	$K   K = kP_B.$
3.Computes $SK = wK$ and $S_m = wH(SK  t  n$	ı).
	<i>t</i> , <i>m</i> , $S_m$ 4. Computes $Q_B = H_1(ID_{BV})$ , $SK = kQ_L$
	Verifies
	$\hat{e}(P_B, S_m) = ? \hat{e}(H(SK  t  m), Q_L),$
	$\hat{e}(Q_B, S) = ?\hat{e}(Q_L, H(c  R  ID_{BV}))\hat{e}(P_B, R),$
	Stores payment record into DB.

Fig. 1. The proposed protocols

**Deposit protocol.** On the end of a business day, merchant M sends **payment records** in batch to bank B for e-cash depositing. For each **payment record**, B takes the following actions.

- (1) verifies the validness of the license  $Q_L$  by examining SIG<sub>T</sub>( $Q_L$ ).
- (2) fetches the corresponding  $Q_B$  and  $P_B$  from its database using the received  $ID_{BV}$ .
- (3) confirms the ownership of the **payment record** by computing  $SK = k \cdot Q_L = kwP_B$  and checking to see if  $\hat{e}(P_B, S_m) = \hat{e}(H(SK||t||m), Q_L)$  holds.
- (4) verifies the validness of the e-cash by evaluating  $\hat{e}(Q_B, S) = ?\hat{e}(Q_L, H(c||R||ID_{BV}))\hat{e}(P_B, R).$
- (5) checks to see if the **payment record** is a duplicate. If so, we impute this misuse to the dishonest M who doubly deposits it.
- (6) checks if the e-cash is over-spent. This means that B will sum all payment amounts relating to the same e-coin c; if the total amount is over the face value, we impute this misuse to the dishonest U who overspends the e-cash.
- (7) If all above checks passed, B accepts the **payment record** and credits m into the M's account.

**Owner tracing protocol.** When *e-cash* is overspent or abused by criminals and these misuse behaviors have been determined or are undergoing investigation by the court, *B* or a law enforcement agency can request trustee *T* to revoke the anonymity of the *e-cash*. As we know that *e-cash* must be presented with a valid **license**  $Q_L$ , the requestor therefore submits the  $Q_L$  of the suspected e-cash to *T*. Upon receiving  $Q_L$ , *T* retrieves the corresponding record  $\{U, Q_L\}$  from its database and successfully reveals the owner of  $Q_L$ .

# 5 System Analysis and Evaluation

We analyze the proposed system in terms of privacy, security, system functions and fraud prevention.

#### 5.1 Privacy and Security Analysis

Regarding the privacy and security of the proposed e-cash, the following seven questions must be answered.

Question 1. (Anonymity Issue) Can a bank link a specific user to e-cash {c, S, R} between or after a withdrawal process?

In a withdrawal process, bank B first authenticates user U as its account holder to provide subsequent withdrawal services and finally debit U's account. Then, if B can recognize any data items in the yielded e-cash, say c, S or R (all items indeed *are not* revealed to B in the withdrawal process.), it would be able to link the e-cash to the user U. From this observation, we must examine the data items one by one as follows:

- (1) Item *c* cannot be recognized as it is hidden in the one-way hash function *H*(.) and shuffled by both *U*'s one-time random numbers: secrecy *b* and blind factor *R'*, i.e., *c* is transformed into a blind message  $M = b(H(c||R||ID_{BV}) + R)$ .
- (2) Items S and R cannot be known by B, since U does not reveal them in and after the withdrawal process.

Question 2. (Anonymity Issue) Is a bank B able to link the returned e-cash, i.e. a payment record, {c, S, R  $Q_L$ ,  $SIG_T(Q_L)$ ,  $ID_{BV}$ ,  $P_B$ , k, t, m,  $S_m$ }, to any previous withdrawal transcript, {M, S'}, and thus link it to the identity of user U?

We examine each data item in a payment record as follows.

- (1) Item c is just a random string and cannot be linked to any withdrawal transcripts.
- (2) Item S (=aS') reveals nothing about S', since the randomly chosen integer a makes the variable S uniformly distributed. Thus S cannot be linked to any specific S'.
- (3) Item R (=wR') reveals nothing, since U randomly chooses point R' makes R uniformly random, and thus cannot be related to any withdrawal transcripts.
- (4) The other items { $Q_L$ ,  $SIG_T(Q_L)$ ,  $ID_{BV}$ ,  $P_B$ , k, t, m,  $S_m$ } are never seen in the withdrawal message flows, so it cannot be linked to any previous withdrawal transcripts as well.

To summarize the analysis of the above two questions, we conclude that the bank cannot link e-cash to any particular user. Therefore, we claim that the proposed e-cash system possesses untraceability and thus assure users' privacy.

Question 3. (Unforgeability Issue) Can user U forge e-cash by only using his/her registered license  $Q_L$  without the bank's involvement?

In this case, the user U does not have any advantage since if he/she did so, he/she would be traced through the disclosure of  $Q_L$ . However, criminals (or malicious customers) might use a dummy account to gain some advantages. If a criminal registers a license key w on the trustee, and thereby obtains a valid license  $Q_L = wP_B = wxQ_B$ , can he successfully forge valid e-cash  $\{c^*, S^*, R^*\}$  by himself/herself? According to our protocol, the e-cash must pass the e-cash verification of equation **Eq.(1)**, i.e.  $\hat{e}(H_1(ID_{BV}), S^*)$  should be equal to  $\hat{e}(Q_L, H(c^*||R^*||ID_{BV}))\hat{e}(P_B, R^*)$ . We give the derivation in the following.

$$\hat{e} (Q_L, H(c^* || R^* || ID_{BV})) \quad \hat{e} (P_B, R^*) \\
= \hat{e} (wxQ_B, H(c^* || R^* || ID_{BV})) \quad \hat{e} (xQ_B, R^*) \\
= \hat{e} (Q_B, wxH(c^* || R^* || ID_{BV})) \quad \hat{e} (Q_B, xR^*) \\
= \hat{e} (Q_B, wxH(c^* || R^* || ID_{BV})) + xR^*) \\
= \hat{e} (H_1(ID_{BV}), x(wH(c^* || R^* || ID_{BV}) + R^*))$$

should be equal to  $\hat{e}(H_1(ID_{BV}), S^*)$ .

Thus, if a malicious U first chooses an integer for  $c^*$  and a  $G_1$  element for  $R^*$ , then the value  $S^*$  should be equal to  $x(wH(c^*||R^*||ID_{BV}) + R^*)$ . However, U does not have the knowledge of bank B's private key x. So U is unable to forge a valid  $S^*$ to satisfy the verification equation. From another viewpoint, how about the malicious U first determines  $c^*$  and  $S^*$  and then try to find a valid  $R^*$  to satisfy  $R^*$  $= S^* - x(wH(c^*||R^*||ID_{BV}))$ . It is obvious that finding  $R^*$  is hard to due to the one-way properties of the secure hash function and that U has no information about B's private key x.

#### Question 4. (Unforgeability Issue) Can bank B make e-cash by itself?

If bank *B* collects enough spent e-cash including valid license  $Q_L$ , can it use them and *B*'s private key *x* to forge *e-cash* { $c^*$ ,  $S^*$ ,  $R^*$ }? We also observe the equation expansion in the question 3. When malicious *B* first determines an integer as  $c^*$ and a  $G_1$  element as  $R^*$ ,  $S^*$  cannot be computed as  $w(xH(c^*||R^*||ID_{BV}) + R^*)$  due to that *B* has no knowledge about *w*. That is, *B* cannot extract a license key *w* from any collected license  $Q_L$  (=  $wP_B$ ) due to **DL** assumption. Question 5. (Unforgeability Issue) Can an adversary forge valid e-cash?

From Questions 3 and 4, we can easily see that neither a bank which only knows x nor a user who only knows w can successfully forge e-cash.

Question 6. Can an adversary reuse an eavesdropped payment transcript to pay the *e*-cash?

For this question, we argue that only the e-cash owner with a **license key** can generate a valid **owner-signature**  $S_m$  for the payee's one-time random challenge *K*. More specifically,  $S_m$  is analogous to the **BLS** signature where the **license key** is the signing key and the **license** is the verification key. The signature verification tuple { $P_B$ ,  $Q_L$ , H(SK||t||m),  $S_m$ } can be seen as a **VCDH** { $P_B$ ,  $Q_L = wP_B$ ,  $H(SK||t||m) = vP_B$ ,  $S_m = wvP_B$ } tuple for some integer *v*. Thus, we conclude that the **owner-signature**  $S_m$  is as secure as the **BLS** signature which is provably secure.

Question 7. Can an adversary deposit the e-cash eavesdropped from a payment transcript to his/her bank account?

For this, we argue that only the merchant who really participates in the payment transaction can prove that he/she is the payee, because only the true payee knows the discrete logarithm of K in the transcript (This security is based on **DL** assumption.).

#### 5.2 Function Evaluation

We discuss our e-cash system in the features of anonymity, verifiability, unforgeability, bank-off-line, divisibility, anonymity revocation, over-spending prevention, and double-depositing prevention. According to the analysis in Sec. 5.1, anonymity and unforgeability is our system possesses and also anonymity-revocable through the owner-tracing protocol. In addition, it does not need an on-line bank when a payer pays. It therefore is a bank-off-line system. Furthermore, also according to the security analysis, our system can prevent double-depositing. As for the function of over-spending prevention, the following three assurances can guarantee the tracing of the over spenders.

- 1. Our e-cash is **unforgeable**. This implies that no one, including a valid user and the bank, can forge e-cash (see the analysis of Question 3 through 5 in Section 5.1). Valid e-cash must be issued only through a legal withdrawal process.
- 2. The payer must be the e-cash owner in a payment, because only the owner can generate the **owner-signature**, the response to the payee's random

challenge (see the analysis of Question 6).

3. The merchant who can present a valid **payment record** must be the true payee in the payment. (Also see the analysis of Question 7)

Under these three guarantees, when e-cash returns, the bank can believe that this e-cash must be spent by its owner, and that the owner can be traced when needed.

Finally, we discuss the **divisibility** of our e-cash system. For this issue, we adopted a user-self-control approach like the one in the works of Chaum [4] and Fujisaki and Okamoto [19]. We believe that in general, a customer will honestly spend his/her e-cash instead of overspending it. This stems from the fact that e-cash payment is a kind of micro payment, and a user will not take the risk of losing his/her credit for such a small amount of money. Moreover, the above three assurances also guarantee the correct accumulation of the spent money related to a same c. Once overspending occurs, the user will inevitably be traced and his/her credit will be broken.

#### 5.3 Computational Load

In Table 2, we compare the proposed license-issuing, withdrawal, and payment protocols with those of Chen et al.'s [30] in computational load. In the tables, "**P**" indicates a pairing computation, "**M**" a scalar multiplication (which repeatedly adds an elliptic-curve point for specific times, e.g., cP is P + P + ... + P, by adding point P totally c times), "**H**" a hash computation, and "**E**" a symmetric encryption. For computational comparison, we adopt the BLS signature scheme which needs 1**M** and 1**H** for signing, and 2**P** for verifying as our trustee's signature  $SIG_T(.)$ . Table 2 shows the comparison results. As we know that the pairing is expensive in computation time. The cost of a pairing is about 7.5 times of a scalar multiplication on a 3.0GHz Intel Pentium 4 [39], and 22 ~ 38 times on ATmega 128L [40, 41]. The other computations like modular addition, modular multiplications, and elliptic-curve point addition are minor while compared to paring and scalar multiplication. We thus ignore them in the comparison.

Table 2. Computational load comparison						
		Chen et al. 's[30]	Ours			
Lioongo Isquino	Trustee	$1\mathbf{E} + 3\mathbf{M} + 1\mathbf{H}$	$2\mathbf{M} + 1\mathbf{H}$			
License Issuing	User	$3\mathbf{P} + 1\mathbf{M} + 1\mathbf{H}$	$2\mathbf{P} + 1 \mathbf{H}$			
With duran al	Bank	$3\mathbf{P} + 3\mathbf{M} + 1\mathbf{H}$	1 <b>M</b>			
wiinarawai	User	$3\mathbf{P} + 4\mathbf{M} + 1\mathbf{H}$	$3\mathbf{M} + 1 \mathbf{H}$			
Danua aut	Merchant	$3\mathbf{P} + 2\mathbf{M} + 1\mathbf{H}$	$7\mathbf{P} + 2\mathbf{M}$			
Fayment	User	0	2 <b>M</b>			

Table 2. Computational load comparison

From Table 2, we see that our license-issuing and withdrawal protocols are better than Chen et al.'s in computational time. Especially, a user needs not do the time-consuming pairing in withdrawal phase. Our payment protocol needs 2 scalar multiplications for the user and 4 more pairings for the merchant. This is because our payment protocol can resist an adversary reusing any e-cash he eavesdropped while Chen et al.'s scheme cannot. To sum up, our design achieves the goal that the computation at the user side is minimized much more.

# 6 Implementation

We use ASUS S400CS notebook with CPU Intel i5-3317U, 1.7GHz and 4G DDR3 memory. The OS is Linux Ubuntu 10.0. Then we refer the website of Stanford Pairings Based Crypto (PBC) to build PBC library. Before building PBC library, one must install package M4, GMP library, flex, and bison through "apt-get install" tool. Then download PCB source codes from the web, extract them and build the library as follows.

./configure make make install

To verify the library, one can build a sample program, BLS signature.

gcc bls.c -L. -I/usr/local/include/pbc -lpbc -lgmp

Then run the BLS signature and obtain the result as follows.

 $yalin @ Yalin-S400 CA: \label{eq:alpha} cont < ... / param/a. pa$ 

Short signature test

system parameter g =

[511267302110836078778360010027131213113670654026572466298919956587480798170120 6279998578005499322237979804815518272161767325759937954811376023943882181005, 214425445631695375300469331197610454682131399254823583306167880725498330186120 2997065050236389577032107239295513644292181363488981963137319080585542009173] private key = 542559187083824065163733473754519256747925069671 public key =

[520822654980310955221753153234482259236203818177570303347947003305311372172930 1376132039584028061658267261988484532598495357238238176896102687548539221973, 406986460228569599764626921427173158701290707325939952716040330427711626966302 6729113734514777918418252852664280276983591575413943338351976462282613558333] message hash =

[630807567735233679090628126329498672966163176938701969125777863072058930197565 9247632280684514057571723764287112653870734826839929986584710989244826273472, 614245470100850358118887130787970142648781707433864779641665145805386621936826 5234706270304034263890451990757541502223250918907047682554979511124774751109] signature =

[246173939816086888522650850743209096106548661188780158058438995070519216436202 6264713924158259449199309930555941863532657852544755708770237760623103077942, 139561282930240122824108032240448000239607710572875658316851342947817054017088 9284679269142852291134118500899592793476922919176893432610948195432736128712] compressed =

2F00BB45689DA4706D5823387524B6806E03F1A31923B67C11AA28E8BA857DCEB21E13F 7073D13EC65DC6C444E2EA1CBC3537A787E0267F946FB42E5E9EA6E3600 decompressed =

[246173939816086888522650850743209096106548661188780158058438995070519216436202 6264713924158259449199309930555941863532657852544755708770237760623103077942, 139561282930240122824108032240448000239607710572875658316851342947817054017088 9284679269142852291134118500899592793476922919176893432610948195432736128712] f(sig, g) =

[807886587534286735001643733402109636069208383315823415341057775087762267534230 4814930020593497277261414623669343859198563687104717448715478287199790485854, 814997088712056477741664337680614175353387303958700919054154956206256803959895 532119338489939166808431254756310916125210987674806418235389079113929993007] f(message hash, public\_key) =

[807886587534286735001643733402109636069208383315823415341057775087762267534230 4814930020593497277261414623669343859198563687104717448715478287199790485854, 814997088712056477741664337680614175353387303958700919054154956206256803959895 532119338489939166808431254756310916125210987674806418235389079113929993007] signature verifies

x-coord =

2F00BB45689DA4706D5823387524B6806E03F1A31923B67C11AA28E8BA857DCEB21E13F 7073D13EC65DC6C444E2EA1CBC3537A787E0267F946FB42E5E9EA6E36 de-x-ed =

[246173939816086888522650850743209096106548661188780158058438995070519216436202 6264713924158259449199309930555941863532657852544755708770237760623103077942, 738509797036091129419670166234956981341080609368545162786013996978830509070933 3672399356036570371087304654959176788840536358536473884870376729697262096079] signature verifies on second guess random signature doesn't verify

To implement our e-cash program, we adopt type A pairings. Type A pairings are constructed on the curve  $y^2 = x^3 + x$  over the field F\_q for some prime  $q = 3 \mod 4$ . Both G<sub>1</sub> and G<sub>2</sub> are the group of points E(F\_q), so this pairing is symmetric. It turns out  $#E(F_q) = q + 1$  and  $#E(F_q^2) = (q + 1)^2$ . Thus the embedding degree k is 2, and hence  $G_T$  is a subgroup of  $F_q^2$ . The order r is some prime factor of q + 1.

# 7 Conclusion

E-cash is a desire payment tool which links no information about personal account numbers or card numbers and is different from typical financial cards, including credit cards and debit cards. As an interesting result, e-cash solution can resist online payment frauds arisen from account or card number theft / leakage. This paper presented an ID-based certificateless e-cash to attain this goal while considering lower computational load on the user side. Certificateless system can save both the infrastructure building cost and the transaction processing cost. The analysis and evaluation show that the proposed e-cash scheme is of security, privacy preservation, efficiency and is practical for use.

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# Appendix

# I Main Program

//

```
// ID-Based Certificateless Electronic Cash
//
#include <stdio.h>
#include <pbc.h>
#include <pbc test.h>
#include <string.h>
#include <time.h>
int main(int argc, char **argv) {
    pairing_t pairing;
    element_t P;
    element_t x, w, y;
                                 //x: bank's private key, w: user's license key
    element_t Q_B, P_B, Q_L, Y, H_M2G1, SIG_T;
    element_t temp1, temp2;
    char ID BV[] = "FCBKTWTP20141231"; //Bank's identity
    unsigned char data[256];
    int i, len;
```

```
element_t a,b,c,tmpr, RR, R, M, SS, S, tmpG1, tmpG2;
element_t in1[2], in2[2];
element_t k, K, SK, Sm;
time_t curtime;
char datetime[32];
```

```
printf("** E_CASH START **\n");
pbc_demo_pairing_init(pairing, argc, argv);
```

element\_init\_G2(P, pairing); element\_init\_Zr(x, pairing); element\_init\_Zr(w, pairing); element\_init\_Zr(y, pairing); element\_init\_G2(Q\_B, pairing); element\_init\_G2(P\_B, pairing); element\_init\_G2(Q\_L, pairing); element\_init\_G2(Y, pairing); element\_init\_G1(H\_M2G1, pairing); element\_init\_G1(SIG\_T, pairing); element\_init\_GT(temp1, pairing); element\_init\_GT(temp2, pairing);

```
//generate trusstee's private key
element_random(y);
element_printf("Trustee private key y = %B\n", y);
```

```
element_pow_zn(Y, P, y);
element_printf("Trustee public Y = %B\n", Y);
```

```
//generate bank's private key
element_random(x);
element_printf("Bank private key x = %B\n", x);
```

```
//compute Q_B = H(ID_BV)
element_from_hash(Q_B, ID_BV, 16);
printf("Bank ID||VDate = %s\n", ID_BV);
element_printf("Bank public Q_B = %B\n", Q_B);
```

element\_pow\_zn(P\_B, Q\_B, x); element\_printf("Bank public P\_B = %B\n", P\_B); printf("\n------\n"); printf("User -> Trustee :\n"); element\_printf("w = %B\n", w); printf("BankName = FIRST BANK\n"); printf("------\n\n");

//Compute Q\_L & SIG\_T(H(Q\_L))
printf("Trustee fetches bank's identity %s, Q\_B, P\_B\n", ID\_BV);
printf("Trustee Computes license Q\_L...\n");
element\_pow\_zn(Q\_L, P\_B, w);
//Compute SIG\_T(Q\_L)
printf("Trustee signs Q\_L...\n");
len = element\_length\_in\_bytes\_compressed(Q\_L);
element\_to\_bytes\_compressed(data, Q\_L);
printf("computing the hash of Q\_L first\n");
element\_from\_hash(H\_M2G1, data, len);
element\_pow\_zn(SIG\_T, H\_M2G1, y);

```
printf("\n------\n");
printf("Trustee -> User:\n");
    //element_printf("Q_L = %B\n", Q_L);
//len = element_length_in_bytes_compressed(Q_L);
    printf("Q_L(%d bytes compressed in HEX) = ", len);
//element_to_bytes_compressed(data, Q_L);
for(i=0; i<len; i++) {
    printf("%02X", data[i]);
}
printf("\n");
    //element_from_bytes_compressed(Q_L, data);
    //element_printf("decompressed = %B\n", Q_L);
```

len = element\_length\_in\_bytes\_compressed(SIG\_T);

```
//element_printf("SIG_T = %B\n", SIG_T);
    printf("SIG_T(H(Q_L)) (%d bytes compressed in HEX) = ", len);
element_to_bytes_compressed(data, SIG_T);
for(i=0; i<len; i++) {
    printf("%02X", data[i]);
}
printf("\n");
    //element_from_bytes_compressed(SIG_T, data);
    //element printf("decompressed = %B\n", SIG T);
printf("ID BV = %s n", ID BV);
len = element_length_in_bytes_compressed(P_B);
    //element_printf("P_B = %B\n", P_B);
    printf("P_B(%d bytes compressed in HEX) = ", len);
element_to_bytes_compressed(data, P_B);
for(i=0; i<len; i++) {
    printf("%02X", data[i]);
}
printf("\n");
    //element_from_bytes_compressed(P_B, data);
    //element_printf("decompressed = %B\n", P_B);
printf("-----\n\n");
```

```
printf("User verifies SIG_T...\n");
// compute e(SIG_T, P)
element_pairing(temp1, SIG_T, P);
element_printf("computing e(SIG_T, P) = %B\n", temp1);
```

```
// compute e(H(Q_L), Y) should match above
element_pairing(temp2, H_M2G1, Y);
element_printf("computing e(H(Q_L), Y) = %B\n", temp2);
```

```
if (!element_cmp(temp1, temp2)) {
    printf("** Signature SIG_T verifies **\n");
    printf("User stores w, Q_L, SIG_T, ID_BV, P_B\n");
} else {
```

```
printf("*BUG* signature does not verify *BUG*\n");
}
printf("\n*
                                                 *"):
                 E-Cash Withdrawal Phase
element init Zr(a, pairing);
element_init_Zr(b, pairing);
element_init_Zr(c, pairing);
element init Zr(tmpr, pairing);
element_init_G2(RR, pairing);
element_init_G2(R, pairing);
element_init_G2(M, pairing);
element_init_G2(S, pairing);
element_init_G2(SS, pairing);
element_init_G2(tmpG2, pairing);
element_init_G2(in2[0], pairing);
element_init_G2(in2[1], pairing);
element_init_G1(tmpG1, pairing);
element init G1(in1[0], pairing);
element init G1(in1[1], pairing);
element random(c);
element printf("User generates a random coin c = %B\n", c);
element random(b);
element printf("User generates a random blind factor b = %B\n", b);
element div(a, w, b);
                              // b tmpG1, S, tmpr);
element pairing(temp1, tmpG1, Q B);
/// computinf e(H(c||R||ID), Q L) * e(R, P B) = w/a \pmod{r}
    //element mul(tmpr, a, b);
    //element printf("--yalin--examine ab =? w mod r, ab = %B\n", tmpr);
element printf("User computes blind factor a = w/b (mod r) = %B\n", a);
element random(RR);
element printf("User generates a random point R' = %B\n", RR);
element mul zn(R, RR, w);
                              //computing R = w * RR
```

element printf("User computes R = w \* RR' = %B\n", R);

```
//concatenate c||R||ID_BV
len = 0;
len += element_to_bytes(data+len, c);
len += element_to_bytes(data+len, R);
strcpy(data+len, ID_BV); len += strlen(ID_BV);
printf("User concatenates c||R||ID_BV, result lengh = %d\n", len);
element_from_hash(M, data, len);
element_from_hash(M, data, len);
element_printf("H(c||R||ID_BV) = %B\n", M);
//computes b * (H(c||R||ID_BV)+RR)
element_add(tmpG2, M, RR);
element_mul_zn(M, tmpG2, b);
```

```
printf("-----\n");
printf("User -> Bank:\n");
len = element_length_in_bytes_compressed(M);
element_to_bytes_compressed(data, M);
    printf("Blind message M (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) {
    printf("%02X", data[i]);
}
printf("\n");
printf("------\n");</pre>
```

printf("Bank blindly signs on M using its private key x...\n"); element\_mul\_zn(SS, M, x);

```
printf("-----\n");
printf("Bank -> User:\n");
len = element_length_in_bytes_compressed(SS);
element_to_bytes_compressed(data, SS);
    printf("Blind signature S' (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) {
    printf("%02X", data[i]);
}
printf("\n");
printf("------\n");
```

```
element_mul_zn(S, SS, a);
element_printf("User unblind S' to get S = %B\n", S);
```

```
///////// VERIFY E-CASH ////////
// computing e(S, Q_B)
element_set1(tmpr);
element_mul_zn(tmpG1, S, tmpr);
element_pairing(temp1, tmpG1, Q_B);
```

```
// computing e(H(c||R||ID), Q_L) * e(R, P_B)
len = 0;
len += element to bytes(data+len, c);
len += element_to_bytes(data+len, R);
strcpy(data+len, ID_BV); len += strlen(ID_BV);
element_from_hash(in1[0], data, len);
element_mul_zn(in1[1], R,
                            tmpr);
element mul zn(in2[0], Q L, tmpr);
element_mul_zn(in2[1], P_B, tmpr);
element_prod_pairing(temp2, in1, in2, (int)2);
element_printf("e(S, Q_B) = %B\n", temp1);
element_printf("e(H(c||R||ID), Q_L) * e(R, P_B) = %B\n", temp2);
if(!element cmp(temp1, temp2)) {
     printf("** e-cash signature verifies! ** \n");
} else {
    printf("* BUG * e-cash signature does not verify *BUG* \n");
}
```

```
printf("\n-----\n");
```

```
printf("User -> Merchant:\n");
element printf("c = %B", c);
len = element_length_in_bytes_compressed(S);
element to bytes compressed(data, S);
    printf("S (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) printf("%02X", data[i]);</pre>
printf("\n");
len = element_length_in_bytes_compressed(R);
element_to_bytes_compressed(data, R);
    printf("R (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) printf("%02X", data[i]);</pre>
printf("\n");
len = element_length_in_bytes_compressed(SIG_T);
element to bytes compressed(data, SIG T);
    printf("SIG_T (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) printf("%02X", data[i]);</pre>
printf("\n");
printf("ID BV = %s\n", ID BV);
len = element length in bytes compressed(P B);
element to bytes compressed(data, P B);
    printf("P B (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) printf("%02X", data[i]);</pre>
printf("\n");
printf("-----\n\n");
element random(k);
element printf("Merchant selects a random integer k = %B\n", k);
element mul zn(K, P B, k);
element printf("Merchant computes challange K = k * P B = \%B \n", K);
printf("-----\n");
printf("Mechant -> User :\n");
```

len = element\_length\_in\_bytes\_compressed(K);

```
element_to_bytes_compressed(data, K);
```

```
printf("K (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) printf("%02X", data[i]);
printf("\n");
printf("------\n");
```

```
element_mul_zn(SK, K, w);
element_printf("Merchant computes SK = w * K = %B\n", SK);
time(&curtime);
strcpy(datetime, ctime(&curtime));
printf("current date-time t = %s, money to pay m = 35 dollars\n", datetime);
// computing H_M2G1 = H(SK||t||m) & Sm = w * H_M2G1
len = 0;
len += element_to_bytes(data+len, SK);
strcpy(data+len, datetime); len += strlen(datetime);
strcpy(data+len, "35"); len += 2;
element_from_hash(H_M2G1, data, len);
element_mul_zn(Sm, H_M2G1, w);
```

```
printf("------\n");
printf("User -> Merchant :\n");
printf("t = %sm = 35\n", datetime);
len = element_length_in_bytes_compressed(Sm);
element_to_bytes_compressed(data, Sm);
    printf("Sm (%d bytes compressed in HEX) = ", len);
for(i=0; i<len; i++) printf("%02X", data[i]);
printf("\n");
printf("------\n");</pre>
```

//computing SK
element\_mul\_zn(SK, Q\_L, k);
element\_printf("Mechant computes SK = k \* Q\_L = %B\n", SK);
//////// VERIFY Sm ////////
printf("Merchant verifies Owner-Sig Sm...\n");
//computing e(Sm, P\_B)
element\_set1(tmpr);
element\_mul\_zn(tmpG1, Sm, tmpr);
element\_pairing(temp1, tmpG1, P\_B);
```
//computing e(H(SK||t||m), Q_L)
element_pairing(temp2, H_M2G1, Q_L);
element_printf("e(Sm, P_B) = %B\n", temp1);
element_printf("e(H(SK||t||m), Q_L) = = %B\n", temp2);
if(!element_cmp(temp1, temp2)) {
    printf("** Owner-Sig Sm verifies! ** \n");
} else {
    printf("* BUG * Owner-Sig Sm does not verify *BUG* \n");
}
pairing_clear(pairing);
return 0;
```

#### II Program Running Result

}

yalin@Yalin-S400CA:~/libpbc/e-cash\$ run \*\* E CASH START \*\*

\* Initialization Phase \*

#### G1/G2 generator P =

[487666119482807759550055179592886626733232106514300746517518717364 359875395081268139842198427885155344052913236459133961685469243823 7717238195246093226019,

762490711302429057246733707415408060709568393897876593949439316443 269274301137783565265661248778581468799581438636619571284042151757 6597589227053641209074]

<mark>Trustee private key y =</mark>635903116473564397461234714926838056598580820189 Trustee public Y =

[865993400550310835915046144926454917222994842141760448152522765419 357966038219895999678810495125403435241913331847941325932245619254 1331853064127702087429,

473747679512668660693065161639736865611154306369699910767635676834 386113169057593962952030503447318351385557953702734242678567414741 1312327717643997119129] <mark>Bank private key x =</mark> 548436541016353765443383790905715704719289819248 <mark>Bank ID||VDate =</mark> FCBKTWTP20141231

Bank public Q\_B =

[713029847271779280323096769403147641409348123244330220332641765374 787060032525655389005574220397918056737922028311685128725323777322 8531910893969880976921,

442831748101359447326640981315911324001950087098091553568178840019 241452928311577339135739527723121704771946208198544459979858731996 2364069382982313463494]

Bank public P\_B =

[822579153778586875959118761346659997832837576288619285659826445979 450265255664699622841092742947745555179792643231596178410772234546 8676572551348750794328,

198216487274692478141821197943884179224692312715956417792806291146 068907216708180251602998915397722330558992819366719961513360280704 4341549020317275727872]

\*\*\*\*\*\*

-----

User -> Trustee :

w = 246256710187041570016323985253510015150319455623 BankName = FIRST BANK

\_\_\_\_\_

Trustee fetches bank's identity FCBKTWTP20141231, Q\_B, P\_B Trustee Computes license Q\_L... Trustee signs Q\_L... computing the hash of Q\_L first

-----

Trustee -> User:

Q\_L(65 bytes compressed in HEX) = 60DC89487321F22D9A7B188322ADD18FB8467642F120E8F9EF27050CD63D93B0D 16A4D85568F8AFF4B8C2EA066049178CB71B2DF9E33F558D60329FB9CB2ED0801 SIG\_T(H(Q\_L)) (65 bytes compressed in HEX) = 152D3B136E57932659A1A7DC9312FE3EC131EFFB4DB3DB381F784E826B9379869 3068C5C253148CCE62D597D31D50DFC825A430F60FDC43359D9A5E51F75B79A01 ID\_BV = FCBKTWTP20141231

P\_B(65 bytes compressed in HEX) =

9D0ED4DD2B0F976C1FD6EF823A092C0767EDE18E080D8BF20029BDA71DEEA987 AA95CAACBF629A9605E9556CFBB8D59EB08261F0C3DDFF8B25BE5EA917863E580 0

\_\_\_\_\_

User verifies SIG\_T...

computing  $e(SIG_T, P) =$ 

[534425198276325538074528345297692052384380525924357411262263334162 124851922302698952613681236125579457128058283766702903979128743327 2715368156679759462034,

517903279555356446191097597360501482925062984078612531259523088433 067157891702577394611042262951299547090956390023395412713315368122 3030543595678289308716]

computing  $e(H(Q_L), Y) =$ 

[534425198276325538074528345297692052384380525924357411262263334162 124851922302698952613681236125579457128058283766702903979128743327 2715368156679759462034,

517903279555356446191097597360501482925062984078612531259523088433 067157891702577394611042262951299547090956390023395412713315368122 3030543595678289308716]

\*\* Signature SIG\_T verifies \*\*

User stores w, Q\_L, SIG\_T, ID\_BV, P\_B

\*\*\*\*\*

\* E-Cash Withdrawal Phase \*

User generates a random coin c =

229859786435698729346419597517998228279478549616

User generates a random blind factor b =

350147621030694229437750945938883158240074634176

User computes blind factor  $a = w/b \pmod{r} =$ 

672221337822737864124167321039711297333182157784

User generates a random point R' =

[208339150251225073180861170688352822904958569850180484887224787779

454800822898014206375701843616384709730688090412086800528167849733 4936244624736380088883,

700537713448042663242370620838702435409063324206754634512054593192 984555900883104920149359101372339603903259211462056283517330429238 2402142507065117036327]

User computes R = w \* R' =

[552019384225144599692600724614386687958705272002502589072080391701 110653318297132371476136500146271622800763785097698183402165881520 6433605079045627524619,

888081159811895433390970648851634982964706155198386326136796705173 026103462060352186779676181762902923917039556573749718857061177779 626988911962722605917]

User concatenates  $c||R||ID_BV$ , result lengh = 164

 $H(c||R||ID_BV) =$ 

[768382638588699176772870915746733646902109736879561865282938387017 546715664778758122846354750336182890789020172922712104825819051864 1710184809118822059561,

719022660030052318116786056849801165111987580490900573682982468792 898740075653417406032973794365904703179904939399987802784539052977 1516059139128091770895]

User computes blind message  $M = b * (H(c||R||ID_BV)+R') \dots$ 

-----

User -> Bank:

Blind message M (65 bytes compressed in HEX) =

4FBDAF5D643C46B1B02A889EE49AD5A847FCD64A4D7965F32E1A8C7625C07FB8B 2CC4D0761CBA816ECA19CFACC2575BF76852E880C9DFC0822C46A266EC0310B00

Bank blindly signs on M using its private key x, generating S'...

-----

Bank -> User:

Blind signature S' (65 bytes compressed in HEX) =

33F429B709506EE625CBD9C4526F85AA7F2FEC6879C59E16148984B8CB898D263 FC005A0B23913FB2BC43D9FC50A6D610E1C26D9AB7436768C6D62EC3332E43501

\_\_\_\_\_

User unblind S' to get S =

[944697364895033223248888705842014480473916566985460977823776808364 209959291656405963349991286962686276524130942811432606948110037700 065076792317476132931,

711927088636478628811160727761905351862137478401698085056450474481 812272267504424271835119388068630223507040902571858540309640977374 0758073932590254169601]

 $e(S, Q_B) =$ 

[845032566366455626836352445298271610137426121678762566870859020042 023267847307130676739867197366396591422081613052181016310854872260 6076145501165710012942,

549370360600825769328763026291678160945237288831374727209105826036 313128606946226250844247186498005170694393578263779410147953909513 4827387542368343456411]

 $e(H(c||R||ID), Q_L) * e(R, P_B) =$ 

[845032566366455626836352445298271610137426121678762566870859020042 023267847307130676739867197366396591422081613052181016310854872260 6076145501165710012942,

549370360600825769328763026291678160945237288831374727209105826036 313128606946226250844247186498005170694393578263779410147953909513 4827387542368343456411]

\*\* e-cash signature verifies! \*\*

\*\*\*\*\*\*

\* E-Cash Payment Phase

\*\*\*\*\*\*

\_\_\_\_\_

User -> Merchant:

c = 229859786435698729346419597517998228279478549616S (65 bytes compressed in HEX) =

120995A3E4298933CBF2CC52C323CE63EDDFCE062116785939A40221D853C7B03 0065F376909D3B67BC84501D962CB540B76AEE6072DD83B59734B03E788D84301 R (65 bytes compressed in HEX) =

6966253BCAF9DCC9A5376A153D370E731E771BFBA2BEDFBAA402602B1557DDFA 78087858DC4A67274A7A5731AF81F112B8C243C1BB849FBA6AB71F720B8D360B0 1

SIG\_T (65 bytes compressed in HEX) =

152D3B136E57932659A1A7DC9312FE3EC131EFFB4DB3DB381F784E826B9379869 3068C5C253148CCE62D597D31D50DFC825A430F60FDC43359D9A5E51F75B79A01 ID\_BV = FCBKTWTP20141231

P\_B (65 bytes compressed in HEX) =

9D0ED4DD2B0F976C1FD6EF823A092C0767EDE18E080D8BF20029BDA71DEEA987 AA95CAACBF629A9605E9556CFBB8D59EB08261F0C3DDFF8B25BE5EA917863E580 0

\_\_\_\_\_

Merchant selects a random integer k =

18649282338605649679143610364743564084513103988

Merchant computes challange  $K = k * P_B =$ 

[412913546272363167464976483044576119613212585226835436313606656600 493822571034197390308133908888399332640549082312155143676705498360 180576992643301162861,

534655301753509910304372572596421102277742959845735600870346919806 941073558578959541440877647195468286820618429643807074462844612879 1539893320624511125702]

-----

Mechant -> User :

K (65 bytes compressed in HEX) =

07E24784EC17F4DA0C934A4E8867DCA2FE4867850F50BCB11DC2CA8E7568FE57D FDD59144BDB6DFD4C3BCF0F38D6A6D7BA5C46DC7428AF3200578228634ABF6D0 0

\_\_\_\_\_

Merchant computes SK = w \* K =

[264233210388512968232936937755055870849925035383952005337918855071 191794965027946429005359088116291242770468834356591868091204530100 0484730251535219221754,

216844492079161359973624149302597267242427111004975324786180622714 503171035303652349983871741040452218328256491486886845565148708408 3793886443555136790277]

current date-time t = Sat Aug 30 15:50:50 2014

money to pay m = 35 dollars

User -> Merchant : t = Sat Aug 30 15:50:50 2014 m = 35 Sm (65 bytes compressed in HEX) = A76BC9261FC0B7A5E4F2F145A57B0D8A5256A40FF85B4E9C18EA7DAA5C5611CC5 D64926337DB15D63F3FB3D2EDFC169DFAB3A6DED69660EFBCC95ABC1F9403440 0

Mechant computes  $SK = k * Q_L =$ 

[264233210388512968232936937755055870849925035383952005337918855071 191794965027946429005359088116291242770468834356591868091204530100 0484730251535219221754,

216844492079161359973624149302597267242427111004975324786180622714 503171035303652349983871741040452218328256491486886845565148708408 3793886443555136790277]

Merchant verifies Owner-Sig Sm...

 $e(Sm, P_B) =$ 

[425068860357981089596962294169322312370887301815531313712574904540 986324376205445741372728372636055241228170806326010130356638150382 3723879076875469041752,

101108532973727731818722120810025248298489972424833633257428130925 788151386421385521321301487875887982634053133179843308035316947615 4408678199591543736626]

 $e(H(SK||t||m), Q_L) = =$ 

[425068860357981089596962294169322312370887301815531313712574904540 986324376205445741372728372636055241228170806326010130356638150382 3723879076875469041752,

101108532973727731818722120810025248298489972424833633257428130925 788151386421385521321301487875887982634053133179843308035316947615 4408678199591543736626]

\*\* Owner-Sig Sm verifies! \*\*

Merchant verifies E-Cash...

 $e(S, Q_B) =$ 

[845032566366455626836352445298271610137426121678762566870859020042 023267847307130676739867197366396591422081613052181016310854872260 6076145501165710012942,

549370360600825769328763026291678160945237288831374727209105826036

313128606946226250844247186498005170694393578263779410147953909513 4827387542368343456411]

 $e(H(c||R||ID), Q_L) * e(R, P_B) =$ 

[845032566366455626836352445298271610137426121678762566870859020042 023267847307130676739867197366396591422081613052181016310854872260 6076145501165710012942,

549370360600825769328763026291678160945237288831374727209105826036 313128606946226250844247186498005170694393578263779410147953909513 4827387542368343456411]

\*\* E-Cash verifies! \*\*

C 🖌 🗋 sdiwc.net/conferences/2014/digitsec2014/keynote-speaker/



Q ☆ Ξ

#### Jue-Sam Chou & Yalin Chen Info. Mgmt., Nanhau University C & C Info. Security LAB. ChiaYi, Taiwan

Anonymous **Electronic Cash** Against CNP & Identity Theft

> Yalin Chen and Jue-Sam Chou DigitalSec2014



- Part 1 Background and Motivations
- Part II The Proposed Scheme

#### Taiwanese Payment Methods for Online Shopping, 2012



#### **Taiwan Credit Card Frauds**



Data from Taiwan Joint Credit Information Center.

#### CNP/EC

- In a typical CNP fraud, for example, a cheater offer just a victim's Card No, Card's valid date, and CVC to an online merchant; then he can complete a payment transaction without any error alarms.
- Not-Face-to-Face payment usually happened in the cyber world.
- This is because these card information are easily be collected by the criminals through
  - Trojan Horse, skimming, hacker's hacking merchant's web site, DB or illegal deal

#### Australia Plastic Card Frauds



Data from Australian Payment Clearing Association.

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#### Canada Credit Card Frauds



Data from http://www.kubera.cc

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#### **UK Credit Card Frauds**



http://www.popcenter.org/learning/60steps/index.cfm?stepNum=11

# **Our Countermeasure NOT to Present** Card No. or Identity Anonymous Electronic Cash

# Anonymous Electronic Cash

- Like paper cash which itself is identifiable
  - For E-Cash, one can identify it by verifying the issuer's digital signature
- Untraceability
  - No one can link a presented e-cash to any particular person; this protects individuals' privacy
- E-Cash is typically a series of meaningless bits which link to nothing,
- Not like a card number which always links to a personal identity.

#### E-Cash Types

#### Type I: Bank-controlled E-Cash

Mondex

#### Type II: P2P- distributed (Bank-free) E-Cash

• Bitcoin

#### Type-I: Bank-Controlled E-Cash



# Type-I: Bank-Controlled E-Cash

- Trust payment tool, transactions guaranteed by the banks
- High transaction process fee
- MONDEX
  - o by National Westminster Bank in the U.K.
  - o great success in 1990s, absolute anonymity
  - But open a perfect channel for criminals to untraceably transfer their illegal funds

#### Type-II: P2P BitCoin



# Type II: P2P BitCoin

- Low transaction fee
- Dramatic price  $\rightarrow$  Big risk for the holders
- Hacker attacks  $\rightarrow$  Bigger risk
  - 2014/2 the biggest exchange Mt.gox closed due to 850,000 Bitcoins (about \$4.8b) stolen by hackers
- Privacy issue
  - one may trace sensitive transactions or de-anonymous social network data through using network topology

🗅 www.coin	desk.com/price/					
0000	Coin	Dock		CoinDesk	Bitcoin Price	Index
	The Voice of I	Digital Currency		\$642.40	£382.62 €4	¥4058.81
				Last updated:	Jun 11, 2014 at 17:39	BST
*	NEWS News & analysis	What is bitcoin?	PRICE Current Bitcoin Price	DATA Bitcoin Stats	🛩 f	Q+ 🖸 🔊
Bitcoin > Bitc	oin Price Index					
USD	CNY		Today's Open	\$649.81	Change	\$-7.41 -
<b>\$6</b>	42	40 -	Today's High	\$65A 7A	Market Can	¢0 0750
		-1.14%	loady 5 mgm	\$034.14	market oup	\$0.275D
			Today's Low	\$634 18	Total BTC	12 882 075
7 🔺 🖪	www.xe.com	/currencycharts/	?from=XBL&to=			12,002,010

#### USD per 1 XBT



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As e-cash's public verification key.

### **ID-Based Cryptosystem**

- A Public Key Cryptosystem
- Cheaper transaction handle fee
  - Doesn't need PKI building, maintenance
  - Doesn't need certificate issuing, maintenance, access

RSA

 Public Key
 certificate

 13506641086599522334960321

 62788059699388814756056670

 27524485143851526510604859

 53383394028715057190944175

# Anonymity-evocable E-Cash

- Prevent from money laundry, illegal money transfer
- Legally using e-cash  $\rightarrow$  anonymity maintained
- Illegally using e-cash  $\rightarrow$  anonymity revoked



# Security Bases

- Elliptic Curve Cryptosystem (ECC)
- G is an additive group over a properly chosen elliptic curve. When |G| = q is sufficiently large. It can be used as an ECC.
- **DL problem**: given a group G=<P> and a random point Q in G, it is computationally infeasible to find the integer a such that Q = aP.
- **CDH problem**: given two random points aP and bP in G, calculating abP is computationally infeasible.
- A Secure One-Way Hash function H: y = H(x).

#### <u>p.36</u>

#### **Bilinear** Pairing

- G<sub>1</sub>, G<sub>2</sub>, q, P, e:
- Assume that
  - $(G_1, +)$  and  $(G_2, \cdot)$  are two cyclic groups of order q.
  - $\circ e: G_1 X G_1 \rightarrow G_2.$
  - P is a generator of  $G_1$ , e(P, P) is the generator of  $G_2$ .
- Then
- Bi-linearity:  $e(aP, bQ) = e(P, Q)^{ab}$ .

#### Proposed E-Cash: Notations

x	Bank's private key
$ID_{BV}$	bank's pubic data indicates the bank's identity together with a valid period.
$Q_B$	$Q_B = H_1(ID_{BV})$ is bank's public data
P <sub>B</sub>	$P_B = xQ_B$ is bank's public data
S <sub>T</sub> (.)	Trustee 's signature on some message
W	A user-chosen license key
$Q_L$	$Q_L = wP_B$ is a license for e-cash
SK	a session key shared between the user and merchant in a payment transaction

### Proposed E-Cash System Initialization

- Bank B registers its private key x and its identity with a valid date,  $ID_{BV} = (ID_B, VD_B)$ , to the trustee T.
- B then obtains  $Q_B = H_1(ID_{BV})$ ,  $P_B = xQ_B$  and  $SIG_T(Q_B, P_B)$ , where  $SIG_T(Q_B, P_B)$  is the trustee's signature.
- B publish  $ID_{BV}$ ,  $P_B$  and  $SIG_T(Q_B, P_B)$ .

#### Proposed E-Cash License Issuing Protocol

1. Selects *license key*  $w \in Z_q^*$ .





2. Fetchs the bank's pubic data  $ID_{BV}$ ,  $Q_B$ ,  $P_B$ .

3.Computes  $Q_L = wP_B$ , signs on  $Q_L = S_T(Q_L)$ . License= $\{Q_L, S_T(Q_L), ID_{BV}, P_B\}$ 

#### Proposed E-Cash Withdraw E-Cash Protocol

1. Selects coin *c*, Blind factor *R*', *a*,  $b \in Z_q^*$ such that  $ab = w \mod q$ R = wR',  $M = b(H(c, R, ID_{BV}) + R).$ 




### Proposed E-Cash Payment Protocol

paying \$ m





K

3.Computes 
$$SK = wK$$
,  
 $S_m = wH(SK, t, m)$ 

{
$$c, S, R Q_L, S_T(Q_L), ID_{BV}, P_B, \mathbf{k}, t, m, S_m$$
}





2. Verifies license, Generate a challenge  $K = \mathbf{k}P_{B}$ .

4.  $Q_B = H_1(ID_{BV}), SK = kQ_L$ Verifies the ownership of the **license**  $e(P_B, S_m) =$ ?  $e(H(SK,t,m), Q_L)$ . Verifies e-cash  $(Q_B, S) =$ ?

 $e(Q_L, H(c, R, ID_{BV})) e(P_B, R).$ 5. Write payment record.

p36

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#### Proposed E-Cash Verification Formula

The proposed e-cash verification equation is

 $\hat{e}(H_1(ID_{BV}), S) = ? \hat{e}(Q_L, H(c||R||ID_{BV})) \hat{e}(P_B, R).$ 

We show the proof below.

 $\hat{e}(H_1(ID_{BV}),S)$ 

$$= \hat{e}(Q_B, S)_{\psi}$$

$$= \hat{e}(Q_B, aS')$$

$$= \hat{e}(Q_B, axM)$$

- $= \hat{e}(Q_{B}, axb(H(c||R||ID_{BV}) + R'))_{*}$
- $= \hat{e}(Q_B, \underline{wxH}(c||R||ID_{BV})) \hat{e}(Q_B, \underline{wxR'})$
- $= \hat{e}(wxQ_B, H(c||R||ID_{BV}))\hat{e}(xQ_B, R).$
- $= \hat{e}(wP_B, H(c||R||ID_{BV}))\hat{e}(P_B, R).$
- $= \hat{e}(Q_L, H(c||R||ID_{BV})) \hat{e}(P_B, R).$

 $\hat{e}_{e}^{(P_B, S_m) = e}^{(P_B, S_m) = 0} (H(SK||t||m), Q_I) \text{ holds.}$ 

## Proposed E-Cash Deposit Protocol



payment record: {c, S,  $R Q_L$ ,  $S_T(Q_L)$ ,  $ID_{BV}$ ,  $P_B$ ,  $\boldsymbol{k}$ , t, m,  $S_m$ }

(secure channel)



#### Accept / Reject

(secure channel)

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a. Verifies license Q<sub>L</sub>, S<sub>T</sub>(Q<sub>L</sub>).
b. Verifies the ownership of the payment record by checking k. /\* Bank computes SK = k·Q<sub>L</sub> = kwP<sub>B</sub> and checks (P<sub>B</sub>, S<sub>m</sub>) =? (H(SK||t||m), Q<sub>L</sub>) \*/
c. Verifies E-Cash and the ownership of the E-Cash.
If all are valid, it checks

d. Payment record duplicate?

e. E-Cash is over-spent?

*Q* 1. (Anonymity Issue) Can a bank link to a specific user by e-cash {c, S, R,  $Q_L$ } between or after a withdrawal process?

blind message Mblind signature S'E-Cash= $c, R, S, Q_L$ 

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*Q* 2. (Anonymity Issue) Is bank *B* able to link the returned e-cash, i.e. a payment record, {c, S,  $R Q_L$ ,  $S_T(Q_L)$ ,  $ID_{BV}$ ,  $P_B$ , k, t, m,  $S_m$ }, to any previous withdrawal transcript, {M, S'}, and thus link it to the identity of the user?



Q3. Can user U forge e-cash only by using his/her  $Q_L$  in the registered license without the bank's involvement?



Without knowing the bank's private key x, U will meet a DL problem in computing the e-cash component  $S = x \cdot w \cdot H(c, R, ID_{BV})$ .

Q4. (Unforgeability Issue) Can bank B make e-cash by itself ?



Without knowing license key w, *B* will meet a DL problem in computing  $S = w \cdot x \cdot H(c, R, ID_{BV}).$ 

Q5. (Unforgeability Issue) Can an adversary forge valid e-cash ?

From Q 3 and 4, we can easily see that even a bank which only knows *x* or a user who only knows *w*, cannot successfully forge e-cash.

*Q6. Can an adversary reuse an eavesdropped payment transcript to pay the e-cash?* 



He must compute  $S_m = wH(SK, t, m)$ for a new challenge K. BUT, without knowing the license key w, even he knows the SK, he will meet a CDH problem (p.22). That is, he is unable to compute  $S_m$  to satisfy the license ownership verification(p.28). i.e., Knowing  $vP_B$  (=H(SK,t,m)) for some v, and  $Q_L = wP_B$ , but without knowing the license key wCompute  $S_m = wvP_B = wH(SK, t, m)$  is a CDH problem

Q7. Can an adversary deposit the eavesdropped e-cash from a payment transcript to his/her bank account?

Only the merchant who knows the discrete logarithm of challenge *K* in the transcript can let the bank successively verify the ownership of the **payment record** in the deposit protocol (p.30). Therefore, he will meet a DL problem in computing  $SK = k \cdot Q_L$ To pass the verification  $e(P_B, Sm) =? e(H(SK||t||m), Q_L)$ .

#### Conclusions

- Q1 to Q7 shows the security and privacy preservation of the proposed E-Cash.
- The proposed E-Cash is an ID-based system free from PKI building, maintenance, and access, and thus lower the transaction cost.
- The proposed E-Cash has anonymous property and thus links to nobody.

Therefore is no card No., no identity...

can be stolen.

# Thank You Q & A

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#### 科技部補助計畫衍生研發成果推廣資料表

日期:2014/07/21

	計畫名稱: 防帳卡號被盜之低成本免憑證電子錢網路付款可行性方案研究				
科技部補助計畫	計畫主持人: 周志賢				
	計畫編號: 102-2221-E-343-004-	學門領域: 資訊安全			
	無研發成果推廣	資料			

#### 102 年度專題研究計畫研究成果彙整表

計畫主持人:周志賢 計畫編號:102-2221-E-343-004-							
<b>計畫名稱:</b> 防帳卡號被盜之低成本免憑證電子錢網路付款可行性方案研究							
成果項目			量化	本計畫實		備註(質化 說明:如數個計畫	
		實際已達成 數(被接受 或已發表)	預期總達成 數(含實際已 達成數)	際貢獻百 分比	單位	共同成果、成果 列為該期刊之 封面故事 等)	
	論文著作	期刊論文	0	0	100%	篇	
		研究報告/技術報告	0	0	100%		
		研討會論文	0	0	100%		
		專書	0	0	100%		
	重利	申請中件數	0	0	100%	化	
	子们	已獲得件數	0	0	100%	14	
國內	技術移轉	件數	0	0	100%	件	
		權利金	0	0	100%	千元	
	參與計畫人力 (本國籍)	碩士生	0	0	100%	人次	
		博士生	0	0	100%		
		博士後研究員	0	0	50%		
		專任助理	0	0	100%		
	論文著作	期刊論文	0	0	100%	篇	
		研究報告/技術報告	0	0	100%		
		研討會論文	1	1	100%		獲邀擔任 Plenary Speakers
		專書	0	0	100%	章/本	
	專利	申請中件數	0	0	100%	件	
國外		已獲得件數	0	0	100%		
	技術移轉	件數	0	0	100%	件	
		權利金	0	0	100%	千元	
	參與計畫人力 (外國籍)	碩士生	0	0	100%	人次	
		博士生	0	0	100%		
		博士後研究員	0	0	100%		
		專任助理	0	0	100%		

		獲得優秀論文獎狀一	-張。	
	其他成果			
(無法以量化表達之成				
果如	辨理學術活動、獲			
得獎	填、重要國際合			
作、	研究成果國際影響			
力及	其他協助產業技			
術發	展之具體效益事			
項等	,請以文字敘述填			
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		8		
	成男	<b></b> 果項目	量化	名稱或內容性質簡述
科	成男 測驗工具(含質性與	<b>艮項目</b> 量性)	<b>量化</b> 0	名稱或內容性質簡述
科教	成 測驗工具(含質性與 課程/模組	<b>展項目</b> 量性)	量化 0 0	名稱或內容性質簡述
科教處	<b>成</b> 測驗工具(含質性與 課程/模組 電腦及網路系統或二	L <b>展項目</b> 量性) 工具	量化 0 0 0	名稱或內容性質簡述
科教處計	成男 測驗工具(含質性與 課程/模組 電腦及網路系統或二 教材	L <b>展項目</b> 量性) 工具	量化 0 0 0 0	<b>名稱或內容性質簡述</b>
科教處計畫,	成 測驗工具(含質性與 課程/模組 電腦及網路系統或二 教材 舉辦之活動/證審	<b>K項目</b> 量性) 工具	量化 0 0 0 0	名稱或內容性質簡述 
科教處計畫加坡	成 測驗工具(含質性與 課程/模組 電腦及網路系統或二 教材 舉辦之活動/競賽 研討金/工作技	<b>展項目</b> 量性) 工具	量化 0 0 0 0 0	名稱或內容性質簡述 
科教處計畫加填百	成 測驗工具(含質性與 課程/模組 電腦及網路系統或二 教材 舉辦之活動/競賽 研討會/工作坊 要 2 知 / 細山	L <b>景</b> 性) 工具	量化 0 0 0 0 0 0	<b>名稱或內容性質簡述</b>
科教處計畫加填項日	成 測驗工具(含質性與 課程/模組 電腦及網路系統或二 教材 舉辦之活動/競賽 研討會/工作坊 電子報、網站	L <b>果項目</b> 量性) 工具	量化 0 0 0 0 0 0 0 0	名稱或內容性質簡述 

#### 科技部補助專題研究計畫成果報告自評表

請就研究內容與原計畫相符程度、達成預期目標情況、研究成果之學術或應用價值(簡要敘述成果所代表之意義、價值、影響或進一步發展之可能性)、是否適 合在學術期刊發表或申請專利、主要發現或其他有關價值等,作一綜合評估。

1.	請就研究內容與原計畫相符程度、達成預期目標情況作一綜合評估
	■達成目標
	□未達成目標(請說明,以100字為限)
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	說明:
2.	研究成果在學術期刊發表或申請專利等情形:
	論文:■已發表 □未發表之文稿 □撰寫中 □無
	專利:□已獲得 □申請中 ■無
	技轉:□已技轉 □洽談中 ■無
	其他:(以100字為限)
9	<b>结什舆你才动,</b> 什你创始,礼会影娜领士工,预任顶 <u>你</u> 才田力舆你式 庭田俩
ა.	· 爾依字個成亂、投個創制、在實影審守力॥,計估研充成本之字個或應用俱 值(簡要敘述成果所代表之音義、價值、影變或進一步發展之可能性)(以
	值(前要放延成术///代衣之念我 值值 彩音线运 少孩衣之子能住/代本 500 字為限)
	日前,安全的行動支付工具,已是零售電子商務業者和平台必爭的利器;而
	提供相關支援的軟硬體備廠商等也競相提出各種解決方案。一個電子支付的
	場景如下,使用者用手機掃瞄產品的商品 ORCode,之後在透過第三方支付
	工具扣款,或者利用智手機下載 QRCode 的 App 服務,並完成身份認證與鍵
	入信用卡號後,能隨時用手機行動消費。又例如,手機 Android 系統推出 TSM
	(Trusted Service Manager)平台,讓使用者將信用卡號是鍵入手機內
	SWP-SIM 卡,作為行動支付運作的核心關鍵;蘋果 iOS 系統,在 iPhone 6
	推出 App Pay 服務,準備和 Android TSM 相競抗衡。
	在這樣的背景下,本研究提出的方法和實作正可以提供業者一個安全演
	算法的選擇。我們的方法除了和 RSA 公開金鑰密碼系統一樣安全外 (基於計
	算複雜理論),它的金鑰長度只需要 RSA 金鑰長度的五分之一以下,而且我
	們的方法是 ID-Based 公開金鑰密碼系統, 也就是說允許用身分識別作為公開
	金鑰,例如 Gmail 帳號,銀行的 SWIFT 代碼,業者的官方網址等等。所以,
	我們的方法承接了 ID-Based 公開金鑰密碼系統的好處, 它不需要建置昂貴的
	"公開金鑰基礎建設" (Public Key Infrastrucute, PKI) 來驗證不可讀的"公
	開金鑰"。

RSA 公開金鑰:

Public exponent: 0x10001 Modulus:

13506641086599522334960321627880596993888147560566702752448514

38515265106048595338339402871505719094417982072821644715513736

80419703964191743046496589274256239341020864383202110372958725

76235850964311056407350150818751067659462920556368552947521350

08252879463773285339061097505443349998111500569772368909275623

ID-Based 公開金鑰:

Public key:

Alice@xxx.com

更進一步說,本研究允許全球知名的企業例如 Amazon、Westminster Bank、Citybank,eBay、拉里巴巴等,或地區知名的企業例如 PChome、Yahoo、 義美、台灣銀行等,用其組織的 URL (例如網址)發行自己的匿名電子錢。 也就是讓一些非銀行組織也可擔任第三支付的角色,以活化電子商務金流的 快速流動並降低處理成本。本研究另一個結論是,比起交易成本最低的比特 幣 (Bitcoin),我們的方法提供更安全的電子支付,其處理成本比起現行的信 用卡或透過銀行組織的各式帳卡低廉許多。